

Section 1.1: Variables in Algebra

Variable: a letter that is used to represent one or more numbers Ex: x, y, t, etc.
(*The most popular one is “x”)

Variable Values: the number you substitute in for a variable Ex: Let $x = 4$then $3x = 3(4) = \underline{\hspace{2cm}}$

Variable Expression: a collection of numbers, variables, and operations Ex: $4y$, $8s + 1$, $3x - 4$, $7xy$, etc.
*Expressions DO NOT have _____ signs

Evaluating the Expression: replacing each variable in the expression with a number

Ex: If $x = 3$ $6x =$

Ex: if $y = 9$ $3y - 4 =$

Write the Variable Expression → Substitute Values for Variables → Simplify the Numerical Expression

Ex 1: Let $x = 4$ and $y = -3$ Evaluate $2x + 4y$

Ex 2: Let $p = -6$ and $r = 2$ Evaluate $-3pr$

Ex 3: Let $y = 7$ and $z = -1$ Evaluate $5y - z$

Simple Interest Formula: $I = PRT$

I = Interest Earned

P = _____ Amount (amount of \$ you invest at the start)

R = The Interest Rate Earned (*Rate is ALWAYS plugged in as a _____)

T = Time Period (in _____)

*If you know the principle amount, interest rate, and time period, you can calculate the interest earned!

Ex 1: $P = \$1000$, $r = 4\%$, $t = 3$ years $I =$

Ex 2: $P = \$2500$, $r = 6\%$, $t = 5$ years $I =$

Unit Analysis: Can help determine if your model is correct by showing how the units cancel

*You always need to know the _____ to do unit analysis!

Ex: $12 \text{ in} = 1 \text{ ft}$ $16 \text{ oz} = 1 \text{ lb}$

Section 1.3: Order of Operations

Order of Operations- the order to evaluate expressions with more than one operation

PEMDAS- (Parentheses, Exponents, Multiplication, Division, Addition, Subtraction)

Then **LEFT → RIGHT**

- 1) Parentheses (grouping symbols) first
- 2) Exponents (powers)
- 3) Multiplication/Division from left to right
- 4) Addition/Subtraction from left to right

Ex 1: $2 \cdot 3^2 \div 3$

Ex 2: $4 - (3 - 5)^2 \div 2$

Ex 3: $[4 + (6 - 3)^2 - 9 \div 3]$

Examples with Substitution: Let $x = 3$

Ex 4: $2x - 6 \div 2$

Ex 5: $(2x)^2 - 20 \div (2 + x)$

Examples With Fraction Bars:

- Simplify the top and bottom using PEMDAS, and divide top by bottom or simplify fraction as the last step

Ex 6:
$$\frac{3 + (4 - 2)^3 \div 8}{[20 - (2 - 4)^2 \cdot 4]}$$

Ex 7: Let $x = 2$
$$\frac{3x - 6 \div x + 7}{8 - x + (3 + x) \div 5}$$

Section 1.4: Equations and Inequalities

Equation: Two expressions with an _____ sign (=) between them

Solution of an Equation: If a given value for a variable makes an equation _____, it is a solution!

***Solving an equation means Finding ALL Solutions!**

*To check a solution, plug the value in for the variable and simplify both sides of the equation. If the two sides are equal, the value IS a solution!

Ex 1 : Is 3 a solution to the equation $3x - 2 = 7$?

Ex 2: Is -1 a solution to the equation $4x - 5 = x + 3$?

Using Mental Math Questions:

Ex 3: $x + 4 = 7$ "What number added to 4 is 7?"

Ex 4: $3x = 12$ "Three times what number is 12?"

Ex 5: $x^2 = 25$ "What number squared is 25?"

Inequality Symbols- like an equation, an inequality symbol can be placed between two mathematical expressions

*Substitute in values for the variable, simplify, and determine whether or not the given variable makes the inequality true!

$<$ is " _____ than"

\leq is " _____ than or _____ to"

$>$ is " _____ than"

\geq is " _____ than or _____ to"

Ex 6: Is -2 a solution to the inequality $3x - 4 > 5$?

Ex 7: Is 4 a solution to the inequality $2x - 3 \leq 9$?

Section 1.5: A Problem Solving Plan Using Models

Changing Phrases Into Algebraic Expressions:

Operation	Verbal Expression
Addition	
Subtraction	
Multiplication	
Division	

*The “unknown number” is your variable, usually called x

*"is" means equals.....that is where you put the = in an equation

Operation	Verbal Phrase	Expression
Addition	<p>The <i>sum</i> of 6 and a number</p> <p>Eight <i>more than</i> a number</p> <p>A number <i>plus</i> 5</p> <p>A number <i>increased by</i> 7</p>	
Subtraction	<p>The <i>difference of</i> 5 and a number</p> <p>Four <i>less than</i> a number</p> <p>Seven <i>minus</i> a number</p> <p>A number <i>decreased by</i> nine</p>	

Multiplication	<p>The <i>product of</i> 9 and a number</p> <p>Ten <i>times</i> a number</p> <p>A number <i>multiplied by</i> 3</p>	
Division	<p>The <i>quotient of</i> a number and 4</p> <p>Seven <i>divided by</i> a number</p>	

Translating Word Statements Into Algebraic Equations

Verbal Phrase	Algebraic Equation
Seven more than the product of eight and a number is thirty-one.	
Six less than four times a number is ten.	
Five more than the quotient of twenty and a number is seven.	
Eight multiplied by a number then decreased by three is twenty-nine.	
Nine times the difference between a number and four is fifty-four	
The sum of a number and six, multiplied by two is twenty-eight	

Section 1.6: Tables and Graphs

What is data?

Data: information, facts, or numbers that _____ something

What are some graphical representations we use to display or analyze data?

Bar Graph: _____ or _____ bars used to represent different pieces of data

Line Graph: Data is represented by _____, which may or may not be connected into a _____

***How do you know when to connect the points in a line graph and when NOT to?**

- 1) *A Graph shows number of cd's purchased vs. cost (Not connected)*
- 2) *A Graph shows Time vs. number of miles biked (Connected)*

*Have students come up with their own examples of graphs that should have connected points or not

Section 1.7: An Introduction to Functions

Function: a rule that establishes a relationship between _____ quantities

Input: The number you “put in” (the x-values)

Output: The number you “get out” (the y-values)

*In order to be a function, for every input there must be exactly _____ output!

Are the following tables functions?

X	y
1	4
2	7
3	12
4	19

X	y
1	13
2	15
3	17
3	19

X	y
2	3
4	9
6	3
8	9

Domain: The collection of all the _____ values

Range: The collection of all the _____ values

Tables Should Have:

- Title
- Row Labels (horizontal)
- Column Labels (vertical)
- Key (if needed)

Graphs Should Have:

- Title
- X-axis Label (horizontal)
- Y-axis Label (vertical)
- Key (if needed)
- Scale with _____ !!

Example: Make a table for and graph the following function:

$$y = 250 + 20x$$

$$\text{Domain: } \{0 \leq x \leq 5\}$$

Input (x values)	Output (y values)
0	
1	
2	
3	
4	
5	