

ESSENTIAL QUESTION: How can you verify that a segment is a tangent to a circle?

QUESTIONS:

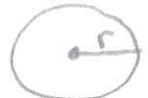
Vocabulary:

Circle
 set of all points in a plane that are equidistant from a given point (center)



Center

Radius
 A segment from the center to a point on the circle



Diameter
 A segment whose endpoints are on the circle and contains the center



Chord
 A segment whose endpoints are on the circle



Secant
 A line that intersects a circle in two pts.



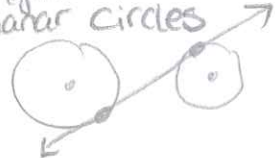
Tangent
 A line that intersects the circle at exactly one point



Coplanar circles
 Circles in the same plane

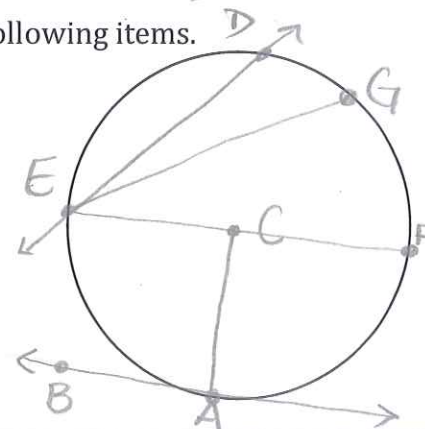


Common tangents
 A line, ray, or segment that is tangent to two coplanar circles



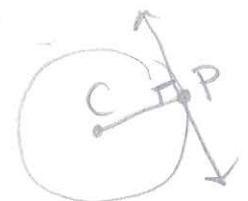
A1. Use the figure at the right to sketch the following items.

- Tangent \overleftrightarrow{AB} , with point of tangency A
- Center C
- Radius \overline{CA}
- Secant \overleftrightarrow{DE}
- Diameter \overline{EF}
- Chord \overline{EG}



SUMMARY:

A tangent to the circle is \perp to the radius of the circle at the endpoint



QUESTIONS:

A2. Use the diagram to find the following...

a. Radius of $\odot A$

$$r = 3 \text{ un}$$

b. Diameter of $\odot A$

$$d = 6 \text{ un}$$

c. Radius of $\odot B$

$$r = 2 \text{ un}$$

d. Diameter of $\odot D$

$$d = 4 \text{ un}$$

e. Radius of $\odot D$

$$r = 2 \text{ un}$$

f. CD

$$1 \text{ un}$$

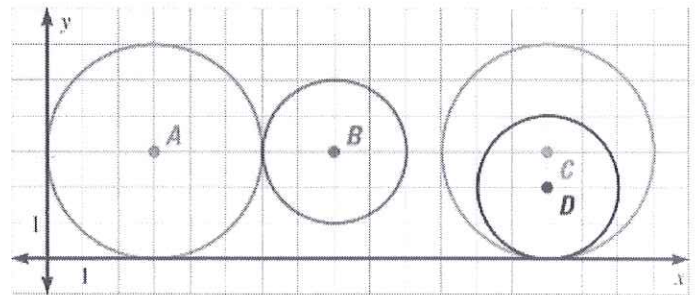
g. BA

$$5 \text{ un}$$

h. Area of $\odot A$

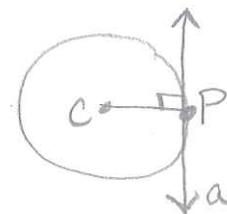
$$\begin{aligned} \text{Area Circle} \\ = \pi r^2 \end{aligned}$$

$$= \pi (3)^2 = 9\pi \text{ un}^2 \approx 28.27 \text{ un}^2$$



Theorem 10.1

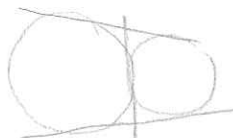
In a plane, a segment, line, or ray is tangent to a circle if and only if it is perpendicular to a radius of the circle at its endpoint on the circle.



line a is \perp to radius \overline{CP}

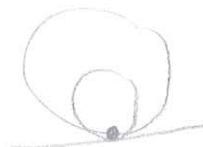
A3. Use the diagram from A2 to find the number of common tangents the pair of circles have.

a. $\odot A$ and $\odot B$



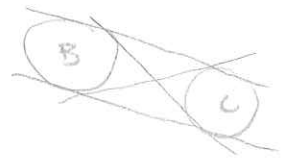
3

b. $\odot C$ and $\odot D$



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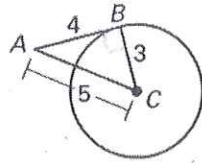
c. $\odot B$ and $\odot C$



4

QUESTIONS:

A4. Determine if \overline{AB} is a tangent of $\odot C$. Explain your reasoning.



Yes,
 $3^2 + 4^2 = 5^2$
 $9 + 16 = 25$

3, 4, 5 is a Pyth. triple
 $\therefore \triangle ABC$ is a rt \triangle with rt $\angle B$

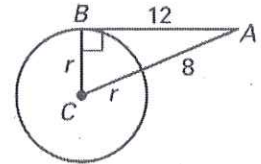
A5. \overline{AB} is a tangent of $\odot C$. Find radius r .

$$r^2 + 12^2 = (r + 8)^2$$

$$r^2 + 144 = (r + 8)(r + 8)$$

$$r^2 + 144 = r^2 + 16r + 64$$

$$\begin{array}{r} r^2 & & & & \\ -r^2 & -64 & -r^2 & & -64 \end{array}$$

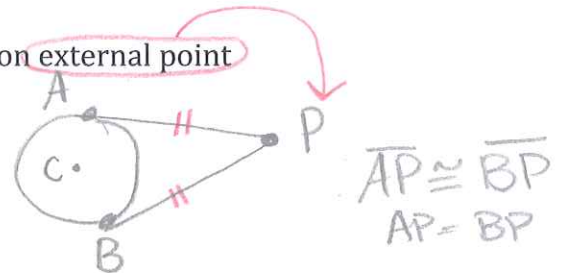


$80 = 16r$
 $r = 5 \text{ in}$

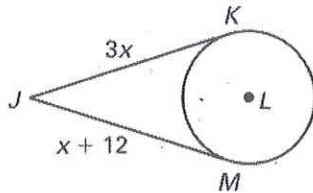
Theorem 10.2

Tangent segments from a common external point

are congruent.



A6. \overline{JK} and \overline{JM} are tangents of $\odot L$. Find the length of \overline{JK} .



$$3x = x + 12$$

$$\begin{array}{r} 3x & & \\ -x & & \\ \hline 2x & = & 12 \end{array}$$

$$x = 6$$

$JK = 3x$
 $= 3(6)$

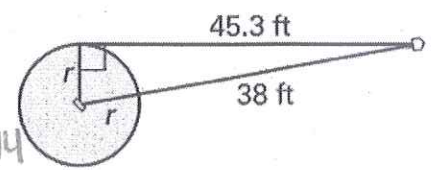
$JK = 18 \text{ in}$

A7. The distance from the edge of softball pitching mound to home plate is 38 feet. Home plate is 45.3 feet to a point of tangency on the pitching mound. Find the diameter of the pitching mound

$$r^2 + (45.3)^2 = (r + 38)^2$$

$$r^2 + 2052.09 = (r + 38)(r + 38)$$

$$= r^2 + 38r + 38r + 1444$$



$$\begin{array}{r} r^2 + 2052.09 = r^2 + 76r + 1444 \\ -r^2 & -1444 & -r^2 & & -1444 \end{array}$$

$608.09 = 76r$ $r = 8.00$ $d = 2(8) = 16 \text{ ft}$

