

Alg III 3.4 (day 2) lesson

Chapter 3 Section 3.4 (Day 2)

EXAMPLE 3

Write the constraints and objective function for the following linear programming problem.

The area of a parking lot is 600 square meters. A car requires 6 square meters and a bus requires 30 square meters. The attendant can only handle 60 vehicles. If a car is charged \$2.50 and a bus \$7.50, how many of each should be accepted to maximize income?

Step #1 Define the variables. Be SPECIFIC!!!

x = number of cars

y = number of buses

* Look at the question
being asked

The area of a parking lot is ~~600~~ square meters. A car requires ~~6~~ square meters and a bus requires ~~30~~ square meters. The attendant can only handle 60 vehicles. If a car is charged ~~\$2.50~~ and a bus ~~\$7.50~~, how many of each should be accepted to maximize income?

x = # of cars

y = # of buses

Step #2

Write the Objective function

- usually involves money

- contains information about maximizing or minimizing

$$C = 2.50x + 7.50y$$

Step #3

Write the constraints. (These are the linear inequalities, look for limitations!)

$$6x + 30y \leq 600$$

* look for common labels

$$x + y \leq 60$$

$$\left. \begin{array}{l} x \geq 0 \\ y \geq 0 \end{array} \right\} \text{common sense}$$

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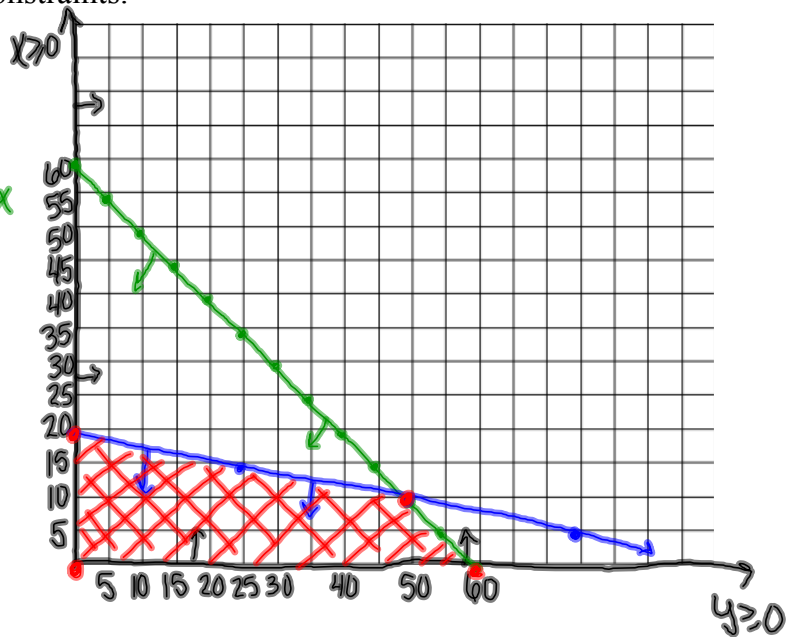
Step #4 Graph the constraints.

$$\left. \begin{array}{l} x \geq 0 \\ y \geq 0 \end{array} \right\} \text{ This means you are in quadrant 1}$$

$$x + y \leq 60 \quad -x \quad y \leq 60 - x$$

$$6x + 30y \leq 600 \quad -6x \quad \frac{30y}{30} \leq \frac{600-6x}{30}$$

$$y \leq 20 - \frac{1}{5}x$$



Step #5 Determine vertices and find max & min values.

Vertices **Value of function** $C = 2.50x + 7.50y$

$$(0,0) \quad C = 2.5(0) + 7.5(0) = \$0$$

$$(0,20) \quad C = 2.5(0) + 7.5(20) = \$150$$

$$(50,10) \quad C = 2.5(50) + 7.5(10) = \boxed{\$200 = \text{max profit}}$$

$$(60,0) \quad C = 2.5(60) + 7.5(0) = \$150$$

Be sure to answer the question being asked

★ **50 cars & 10 Buses will max my profit**